

# Pipelining in Engineering

ENGR 102

Keith M. Chugg

Fall 2015



**USC** University of  
Southern California

# Overview

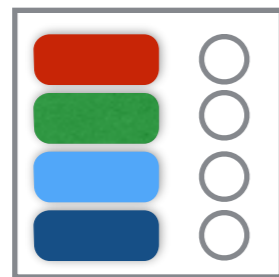
- Explore the concept of pipelining through an example
  - Group reading
- Some reality checks
  - Refining our models
  - Limitations of pipelining
- Characterizing general pipelining approaches

# Group Reading

- 4-page article
- 5 students in the class
- Each student can read 1 page/minute
- *How long does it take for everybody to ready the article?*

# Group Reading - Direct Approach

$T = 0$



student 1



student 2



student 3



student 4

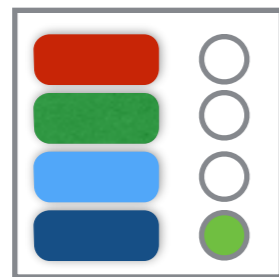


student 5



# Group Reading - Direct Approach

$T = 1$



student 1



student 2



student 3



student 4

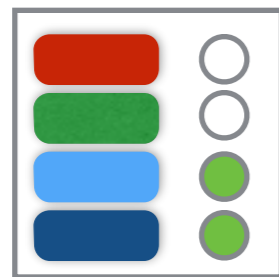


student 5



# Group Reading - Direct Approach

$T = 2$



student 1



student 2



student 3



student 4

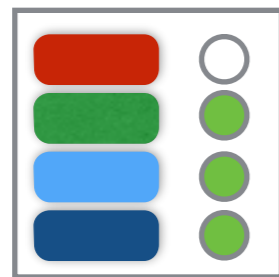


student 5



# Group Reading - Direct Approach

$T = 3$



student 1



student 2



student 3



student 4

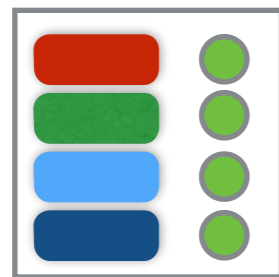


student 5



# Group Reading - Direct Approach

$T = 4$



student 1



student 2



student 3



student 4



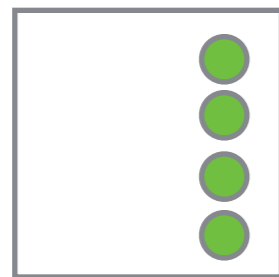
student 5



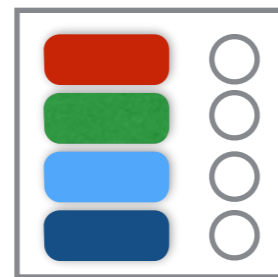


# Group Reading - Direct Approach

$T = 5$



student 1



student 2



student 3



student 4

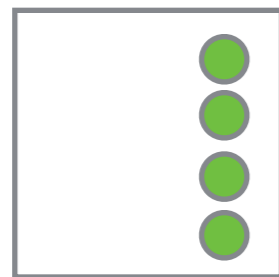


student 5

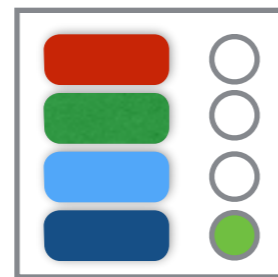
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Direct Approach

$T = 5$



student 1



student 2



student 3



student 4

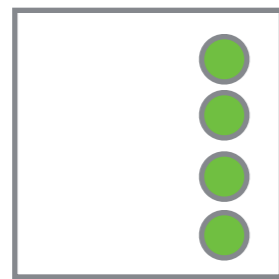


student 5

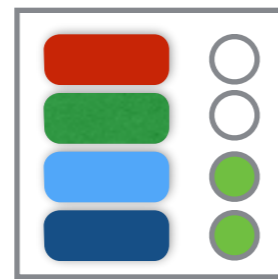


# Group Reading - Direct Approach

$T = 6$



student 1



student 2



student 3



student 4

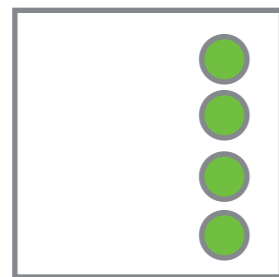


student 5



# Group Reading - Direct Approach

$T = 7$



student 1



student 2



student 3



student 4

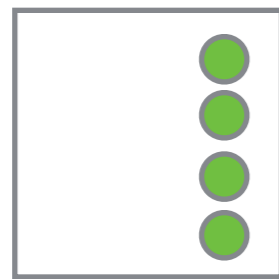


student 5



# Group Reading - Direct Approach

$T = 8$



student 1



student 2



student 3



student 4

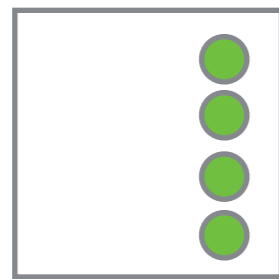


student 5

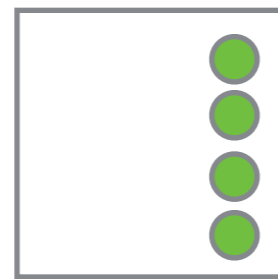


# Group Reading - Direct Approach

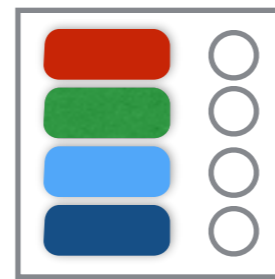
$T = 9$



student 1



student 2



student 3



student 4

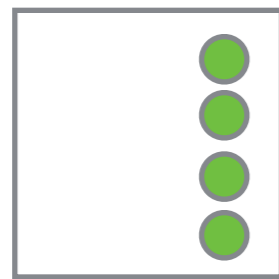


student 5

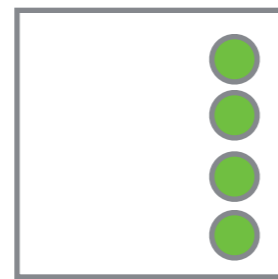


# Group Reading - Direct Approach

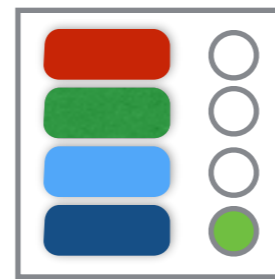
$T = 9$



student 1



student 2



student 3



student 4

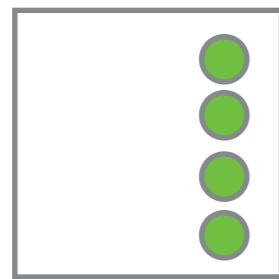


student 5

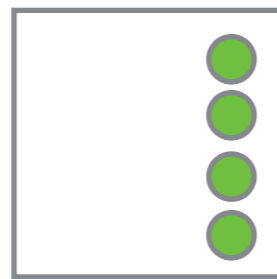


# Group Reading - Direct Approach

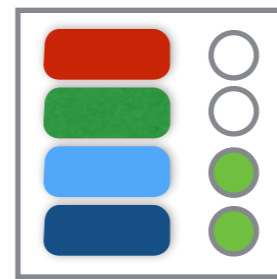
$T = 10$



student 1



student 2



student 3



student 4



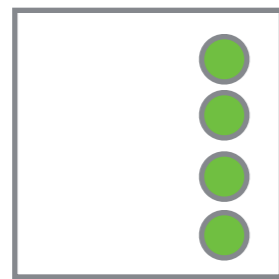
student 5



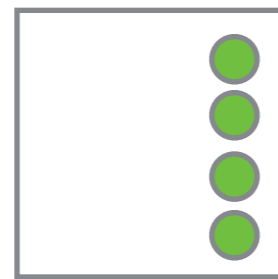


# Group Reading - Direct Approach

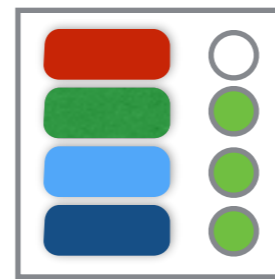
*T = //*



student 1



student 2



student 3



student 4

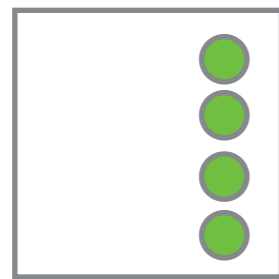


student 5

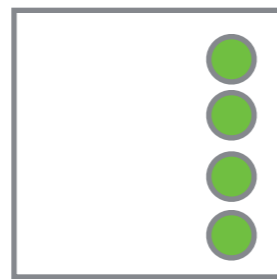


# Group Reading - Direct Approach

$T = 12$



student 1



student 2



student 3



student 4

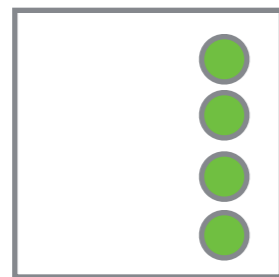


student 5

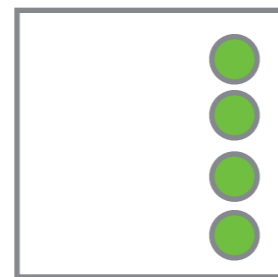


# Group Reading - Direct Approach

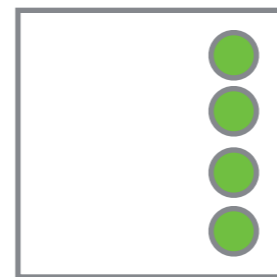
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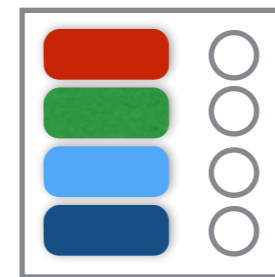
student 1



student 2



student 3



student 4

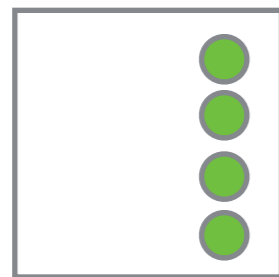


student 5



# Group Reading - Direct Approach

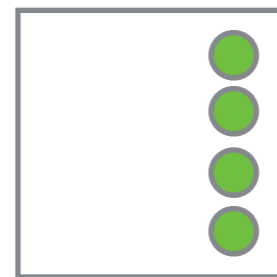
$T = 13$



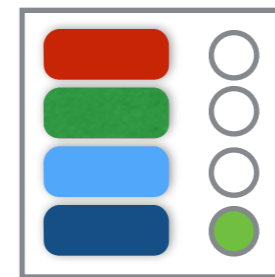
student 1



student 2



student 3



student 4

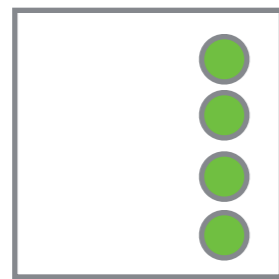


student 5

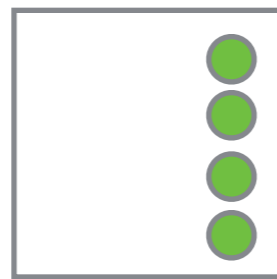


# Group Reading - Direct Approach

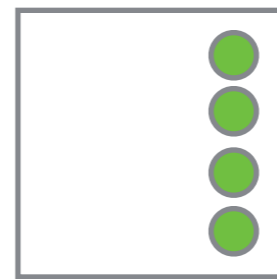
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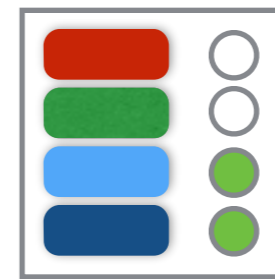
student 1



student 2



student 3



student 4

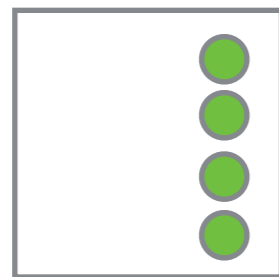


student 5

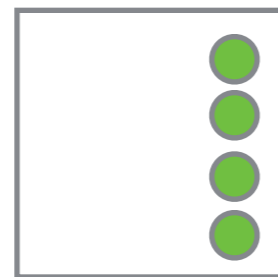


# Group Reading - Direct Approach

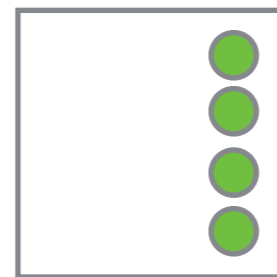
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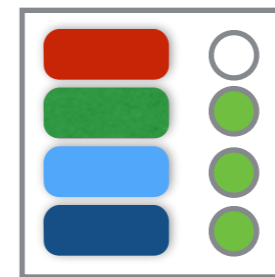
student 1



student 2



student 3



student 4

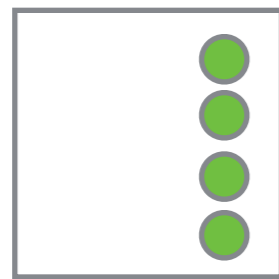


student 5

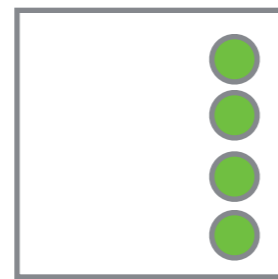


# Group Reading - Direct Approach

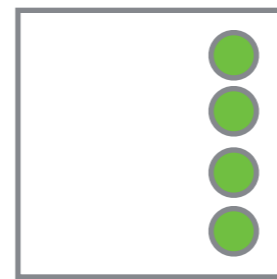
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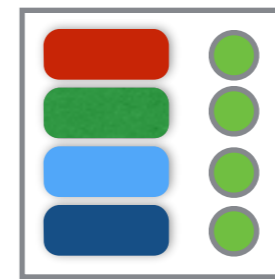
student 1



student 2



student 3



student 4

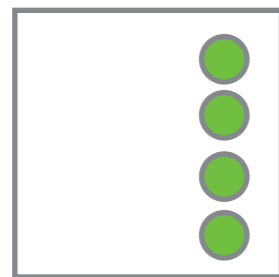


student 5

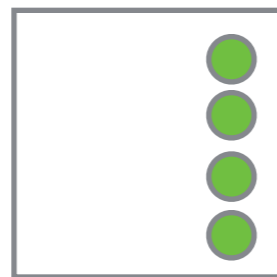


# Group Reading - Direct Approach

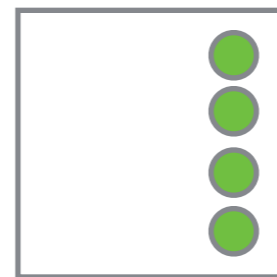
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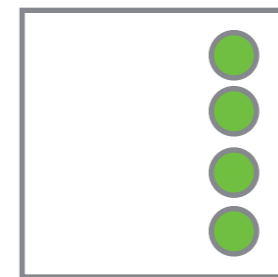
student 1



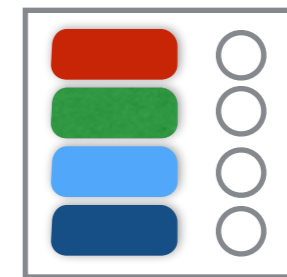
student 2



student 3



student 4



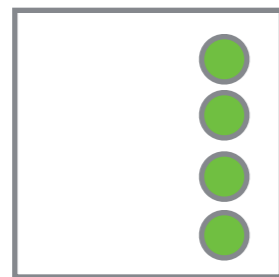
student 5



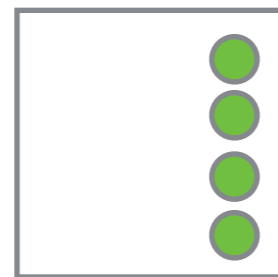


# Group Reading - Direct Approach

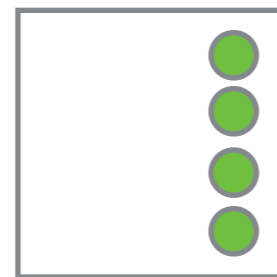
$T = 17$



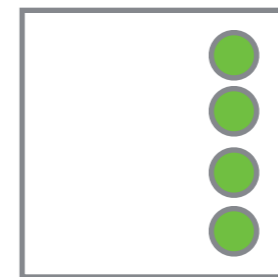
student 1



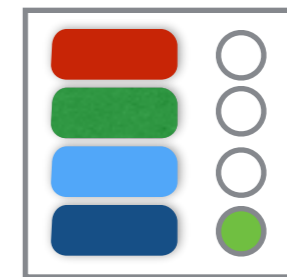
student 2



student 3



student 4

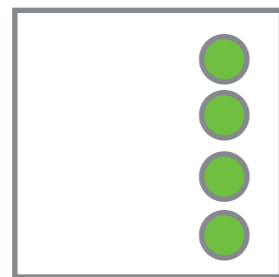


student 5

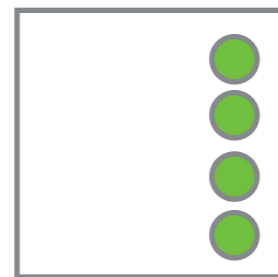


# Group Reading - Direct Approach

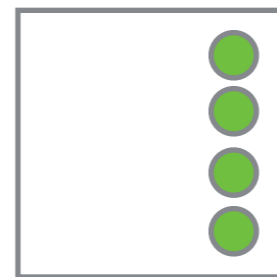
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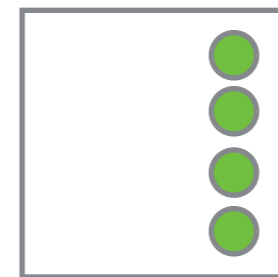
student 1



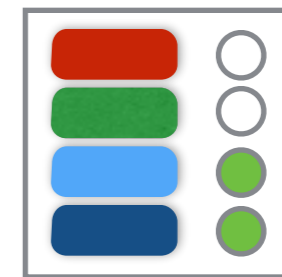
student 2



student 3



student 4

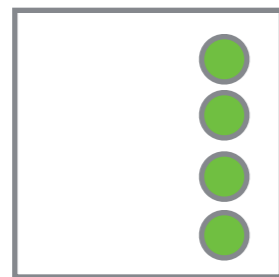


student 5

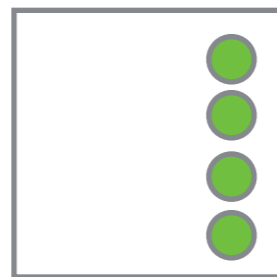


# Group Reading - Direct Approach

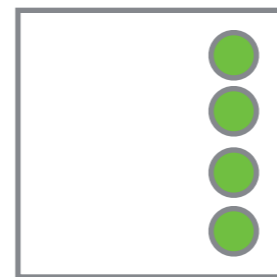
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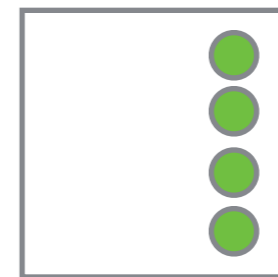
student 1



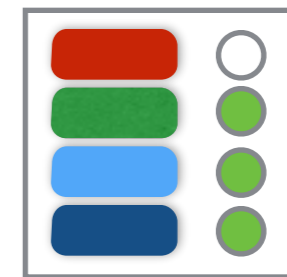
student 2



student 3



student 4

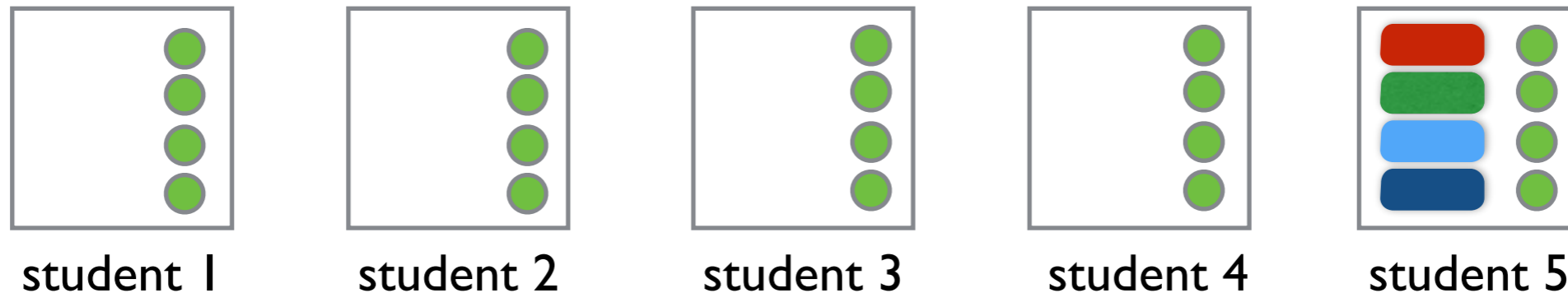


student 5



# Group Reading - Direct Approach

$T = 20$



- *20 time units to complete (mins)*
- *Each student requires 4 time units to complete*
- *Time between one student and the next finishing is 4 time units (mins)*

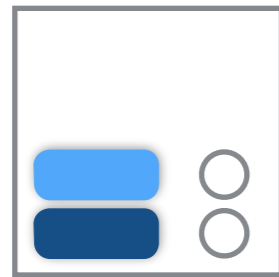
 page 4  
 page 3  
 page 2  
 page 1

# How to speed this up?

- What is slowing us down?
- Distinct methods/concepts:
  - *Parallelism*
  - *Division of labor (job partitioning)*
  - *Pipelining*

# Group Reading - Pipeline with Two Sections

$T = 0$



student 1



student 2



student 3



student 4

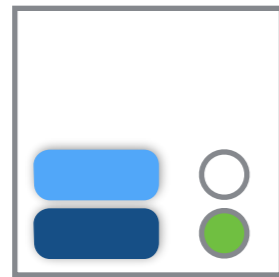


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 1$



student 1



student 2



student 3



student 4



student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 2$



student 1



student 2



student 3



student 4



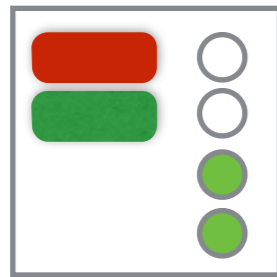
student 5





# Group Reading - Pipeline with Two Sections

$T = 3$



student 1



student 2



student 3



student 4

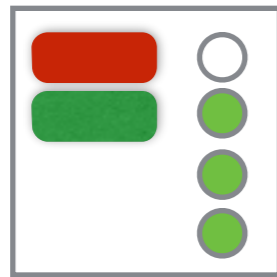


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 3$



student 1



student 2



student 3



student 4

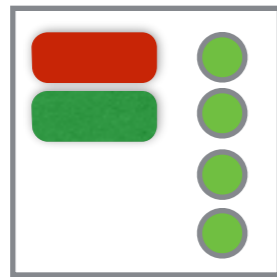


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 4$



student 1



student 2



student 3



student 4

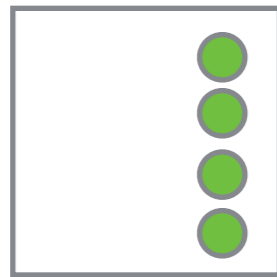


student 5

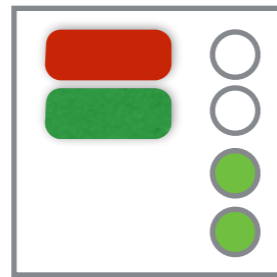
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 5$



student 1



student 2



student 3



student 4

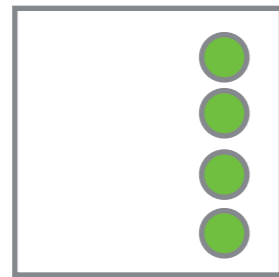


student 5

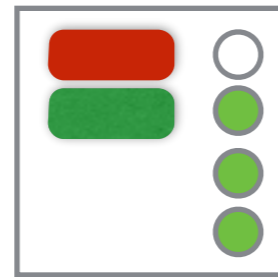
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 5$



student 1



student 2



student 3



student 4

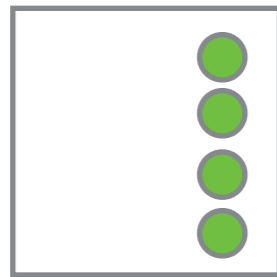


student 5

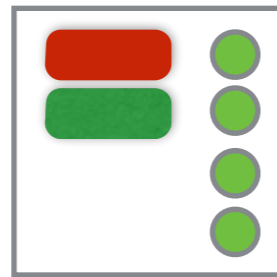


# Group Reading - Pipeline with Two Sections

$T = 6$



student 1



student 2



student 3



student 4

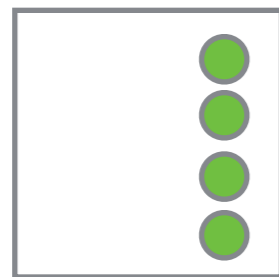


student 5

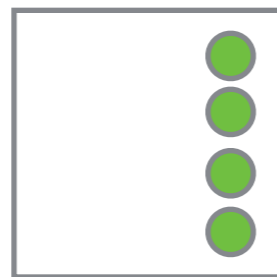


# Group Reading - Pipeline with Two Sections

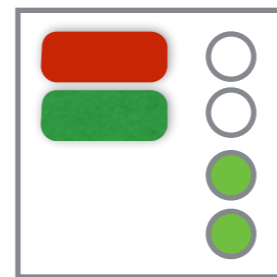
$T = 7$



student 1



student 2



student 3



student 4

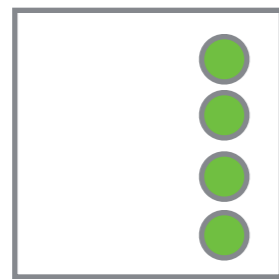


student 5

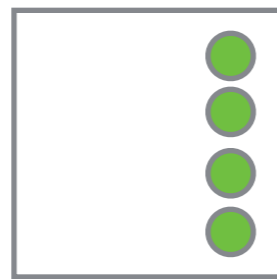
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

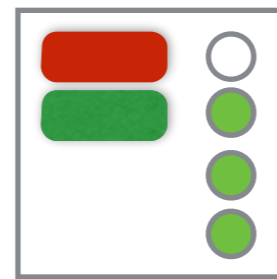
$T = 7$



student 1



student 2



student 3



student 4



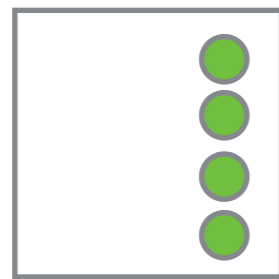
student 5

-  page 4
-  page 3
-  page 2
-  page 1

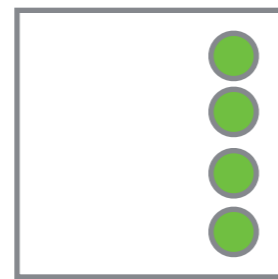


# Group Reading - Pipeline with Two Sections

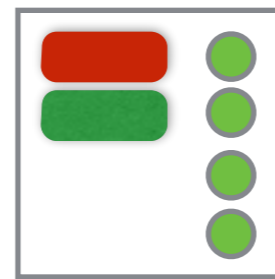
$T = 8$



student 1



student 2



student 3



student 4

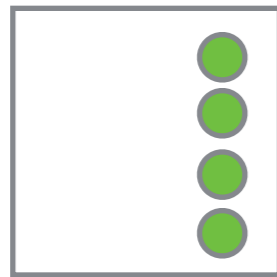


student 5

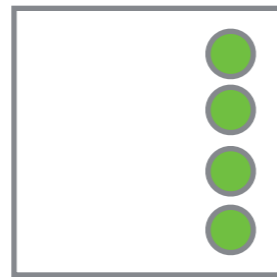


# Group Reading - Pipeline with Two Sections

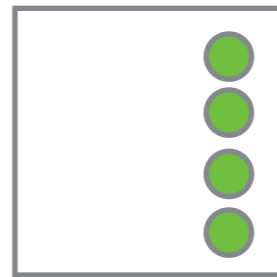
$T = 9$



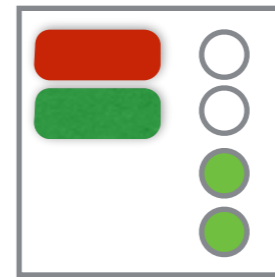
student 1



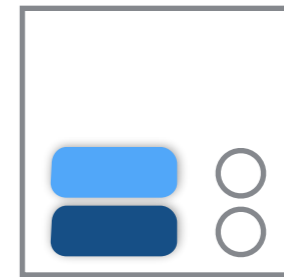
student 2



student 3



student 4

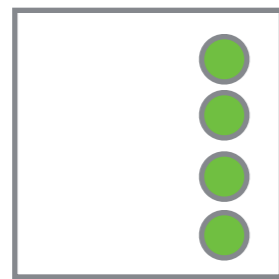


student 5

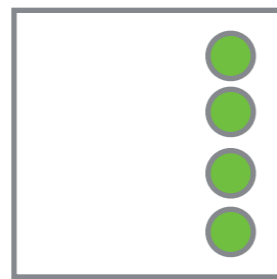
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

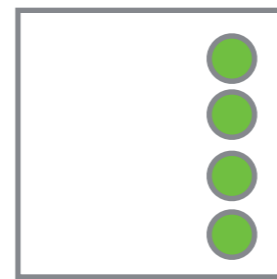
$T = 9$



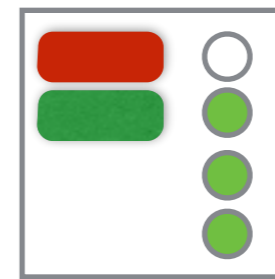
student 1



student 2



student 3



student 4

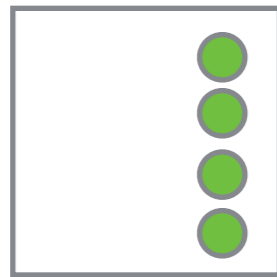


student 5

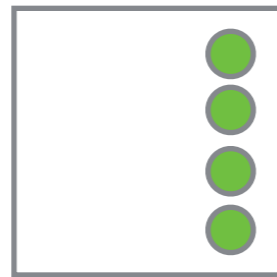
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

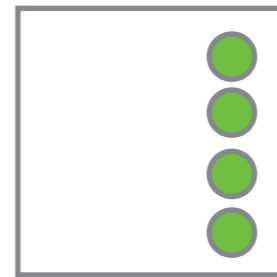
$T = 10$



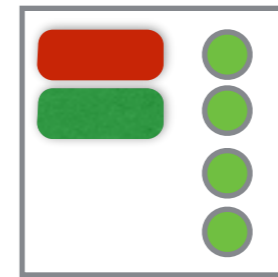
student 1



student 2



student 3



student 4

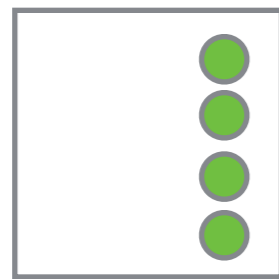


student 5

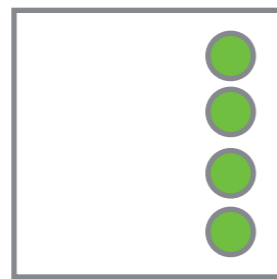
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

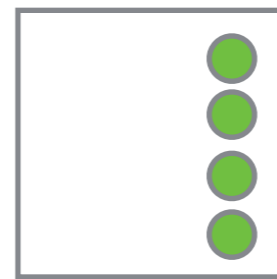
$T = //$



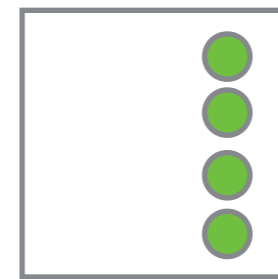
student 1



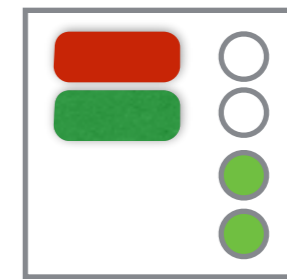
student 2



student 3



student 4

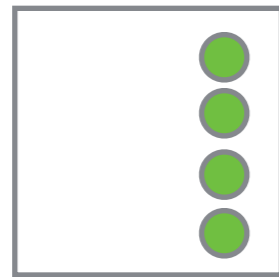


student 5

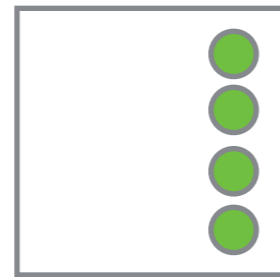
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

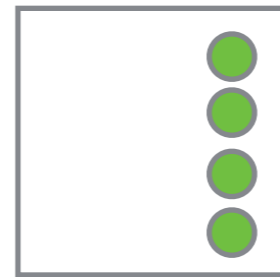
$T = //$



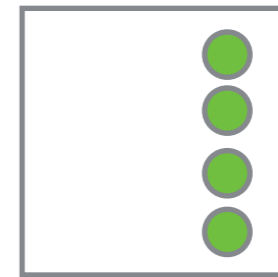
student 1



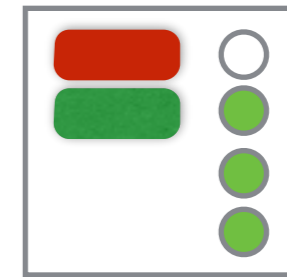
student 2



student 3



student 4

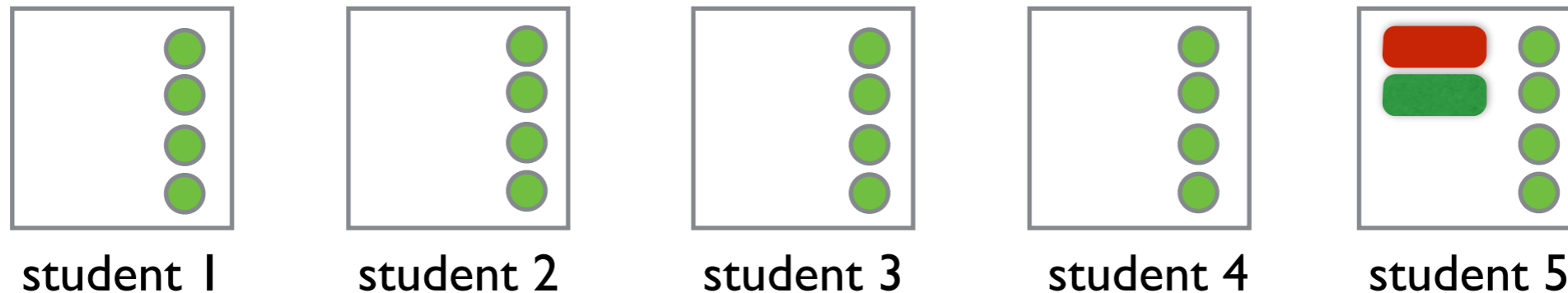


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Two Sections

$T = 12$



- *12 time units to complete (mins)*
- *Each student requires 4 time units to complete*
- *Time between one student and the next finishing is 2 time units (mins)*

# Group Reading - Pipeline with Two Sections

*in words...*

- S1 reads p1&2.
- S1 passes p1&2 to S2.
- S1 reads p3&4, concurrently, S2 reads p1&2.
- S1 passes p3&4 to S2, concurrently, S2 passes p1&2 to S3.
- S2 reads p3&4, S3 reads p1&2.
- S2 passes p3&4 to S3, S3 passes p1&2 to S4.
- S3 reads p3&4, S4 reads p1&2.
- S3 passes p3&4 to S4, S4 passes p1&2 to S5.
- S4 reads p3&4, S5 reads p1&2.
- S4 passes p3&4 to S5.
- S5 reads p3&4.

**Figure 1: A step-by-step description of how five students (S1, S2, S3, S4, S5) read a four-page article partitioned into two 2-page parts (p1&2, p3&4) in a pipelined fashion.**

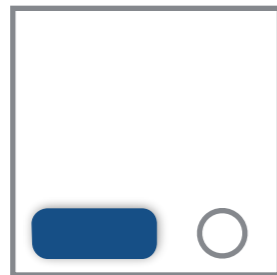


# How to speed this up?

- More of a good thing?

# Group Reading - Pipeline with Four Sections

$T = 0$



student 1



student 2



student 3



student 4

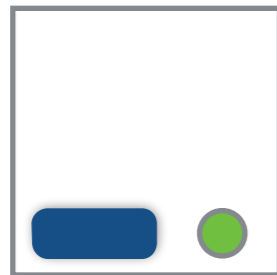


student 5



# Group Reading - Pipeline with Four Sections

$T = 1$



student 1



student 2



student 3



student 4

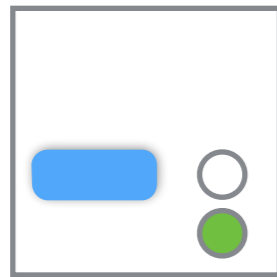


student 5

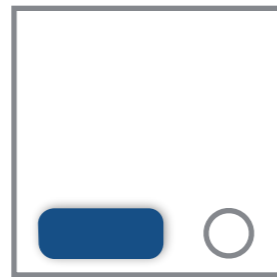
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 2$



student 1



student 2



student 3



student 4

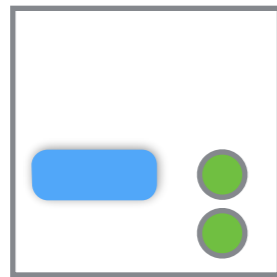


student 5

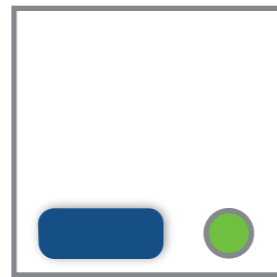
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 2$



student 1



student 2



student 3



student 4

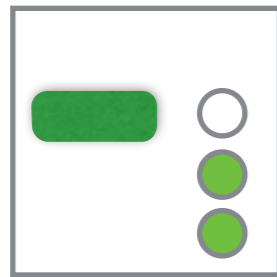


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 3$



student 1



student 2



student 3



student 4

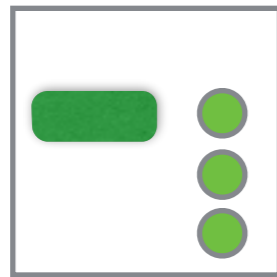


student 5

-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 3$



student 1



student 2



student 3



student 4

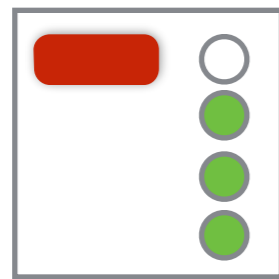


student 5

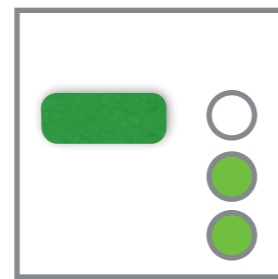
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 4$



student 1



student 2



student 3



student 4



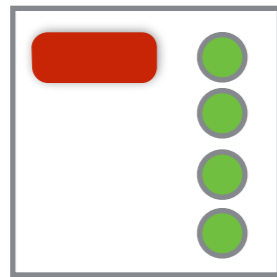
student 5

-  page 4
-  page 3
-  page 2
-  page 1

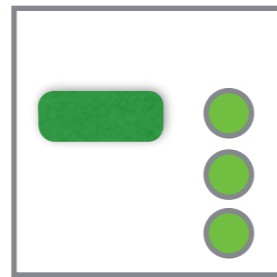


# Group Reading - Pipeline with Four Sections

$T = 4$



student 1



student 2



student 3



student 4

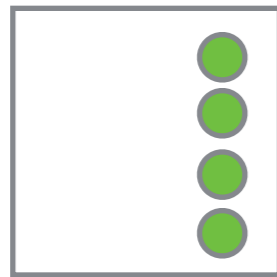


student 5

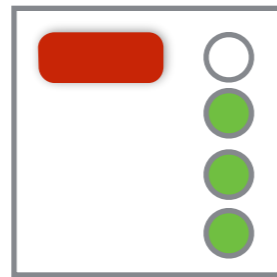
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

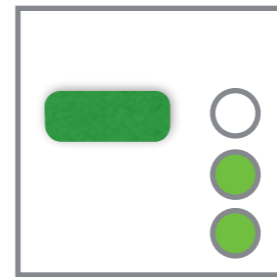
$T = 5$



student 1



student 2



student 3



student 4

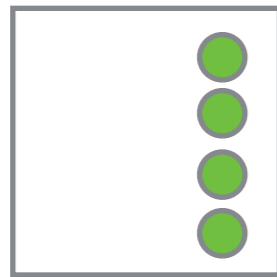


student 5

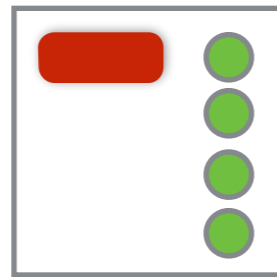
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

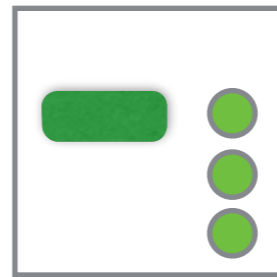
$T = 5$



student 1



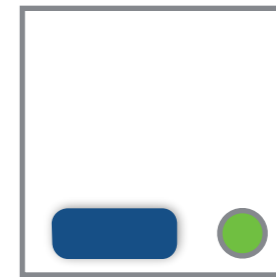
student 2



student 3



student 4

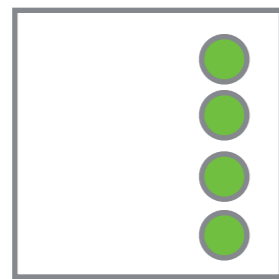


student 5

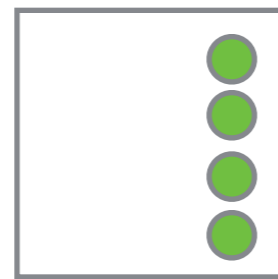
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

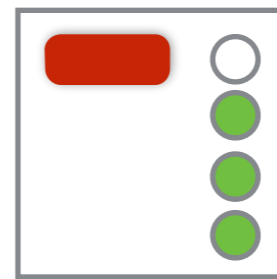
$T = 6$



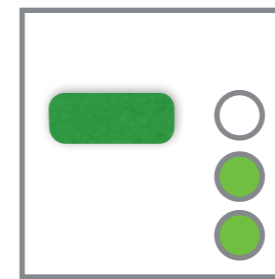
student 1



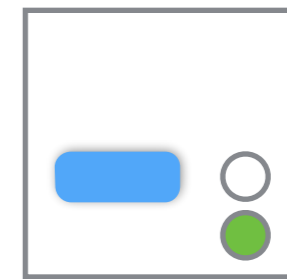
student 2



student 3



student 4

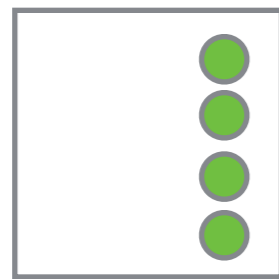


student 5

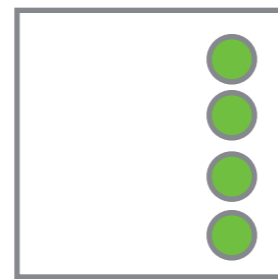
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

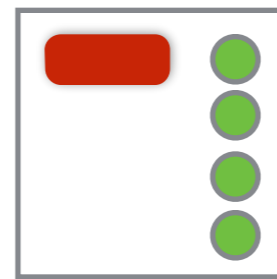
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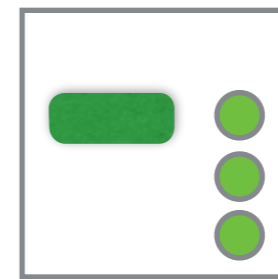
student 1



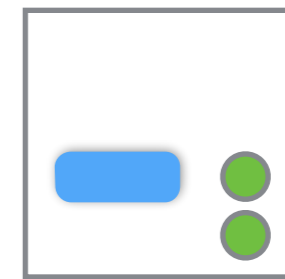
student 2



student 3



student 4

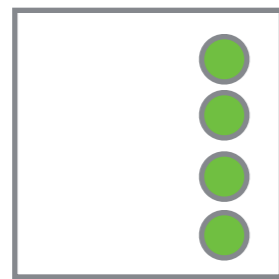


student 5

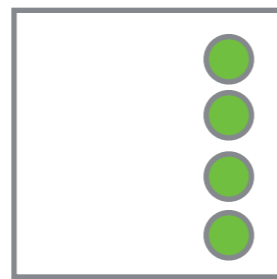


# Group Reading - Pipeline with Four Sections

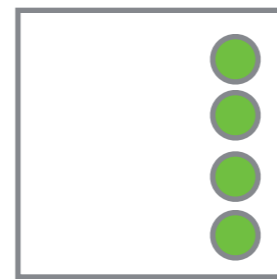
$T = 7$



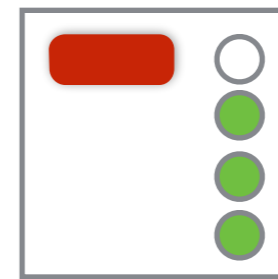
student 1



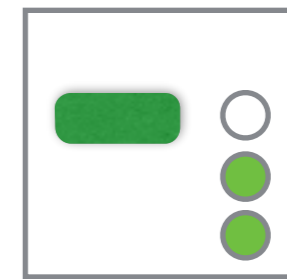
student 2



student 3



student 4

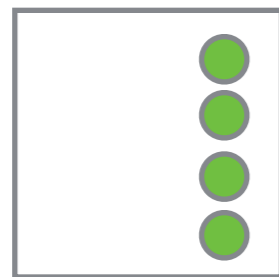


student 5

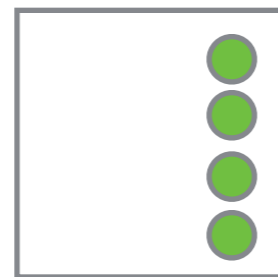
-  page 4
-  page 3
-  page 2
-  page 1

# Group Reading - Pipeline with Four Sections

$T = 7$



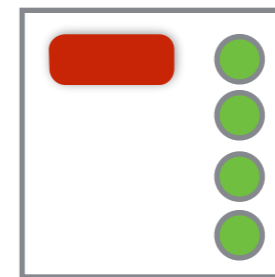
student 1



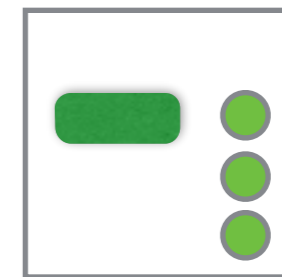
student 2



student 3



student 4

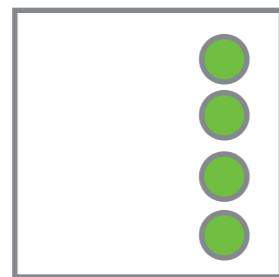


student 5

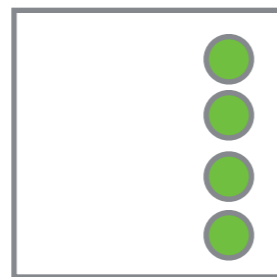


# Group Reading - Pipeline with Four Sections

$T = 8$



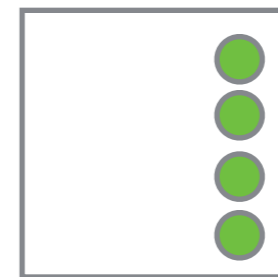
student 1



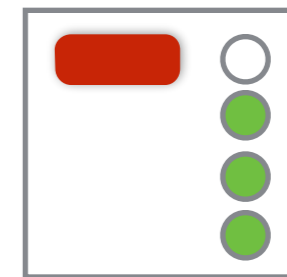
student 2



student 3



student 4



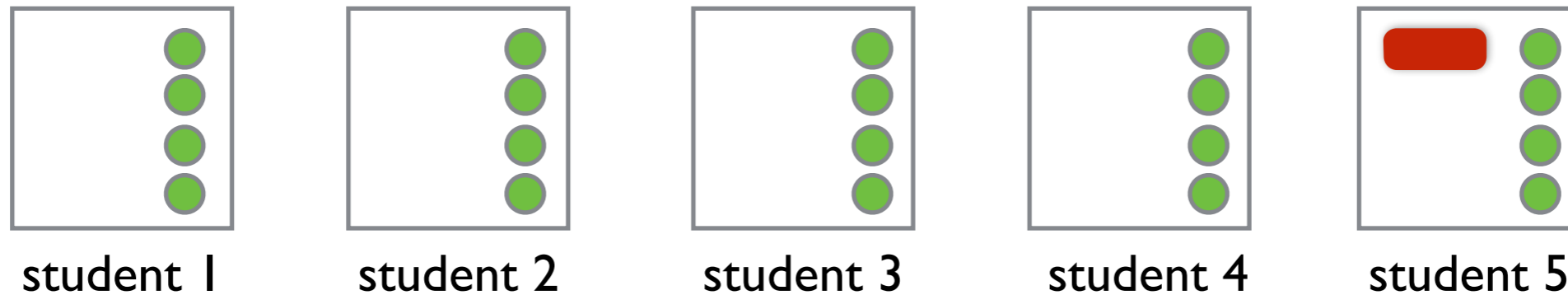
student 5

-  page 4
-  page 3
-  page 2
-  page 1



# Group Reading - Pipeline with Four Sections

$$T = 8$$



- *8 time units to complete (mins)*
- *Each student requires 4 time units to complete*
- *Time between one student and the next finishing is 1 time units (mins)*

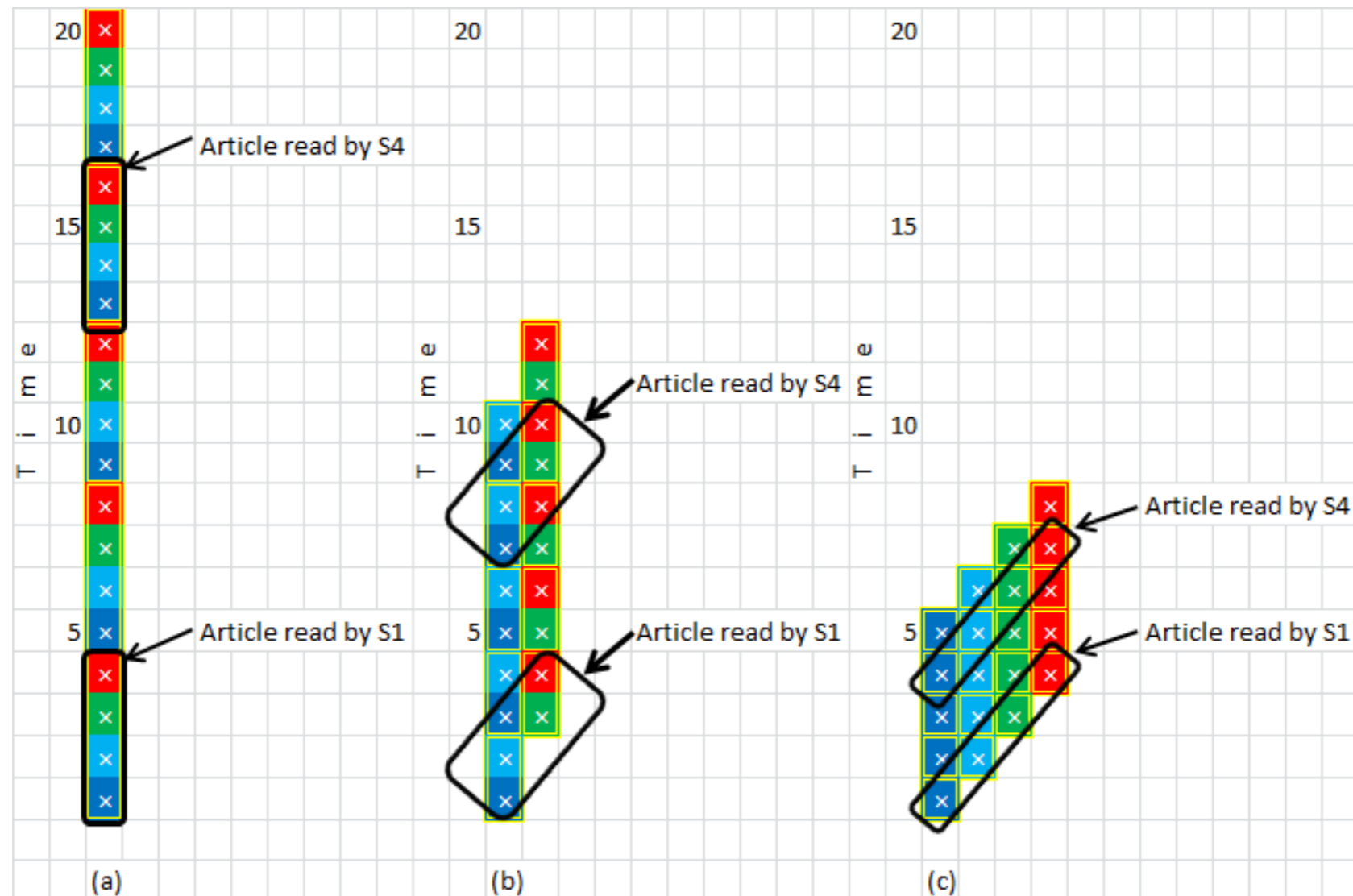
# Group Reading - Pipeline with Four Sections

*in words...*

- S1 reads p1.
- S1 passes p1 to S2.
- S1 reads p2, concurrently, S2 reads p1.
- S1 passes p2 to S2, concurrently, S2 passes p1 to S3.
- S1 reads p3, S2 reads p2, S3 reads p1.
- S1 passes p3 to S2, S2 passes p2 to S3, S3 passes p1 to S4.
- S1 reads p4, S2 reads p3, S3 reads p2, S4 reads p1.
- S1 passes p4 to S2, S2 passes p3 to S3, S3 passes p2 to S4, S4 passes p1 to S5.
- S2 reads p4, S3 reads p3, S4 reads p2, S5 reads p1.
- S2 passes p4 to S3, S3 passes p3 to S4, S4 passes p2 to S5.
- S3 reads p4, S4 reads p3, S5 reads p2.
- S3 passes p4 to S4, S4 passes p3 to S5.
- S4 reads p4, S5 reads p3.
- S4 passes p4 to S5.
- S5 reads p4.

**Figure 3: A step-by-step description of how five students (S1, S2, S3, S4, S5) read a four page article that is partitioned into four 1-page parts (p1, p2, p3, p4) in a pipelined fashion.**

# Comparing these 3 Approaches



**Figure 2: Five students reading one copy of a four-page article at the rate of 1 page per minute. Each box with four squares, two squares, or one square shows a part of the article, and each × indicates the page being read by a student at the particular time indicated by the y-axis. This figure assumes that each passing step takes zero time. (a) Full article read and then passed (non-pipelined, baseline for comparison); (b) article divided into two 2-page parts, each part read and then passed (pipelined); (c) article divided into four 1-page parts, each part read and then passed (pipelined, more extensively than (b)). (For scenarios in (b) and (c), Figure 1 and Figure 3 respectively describe which part is being read by which student at what time.)**

# How to speed this up?

- More of a good thing?

# How to speed this up?

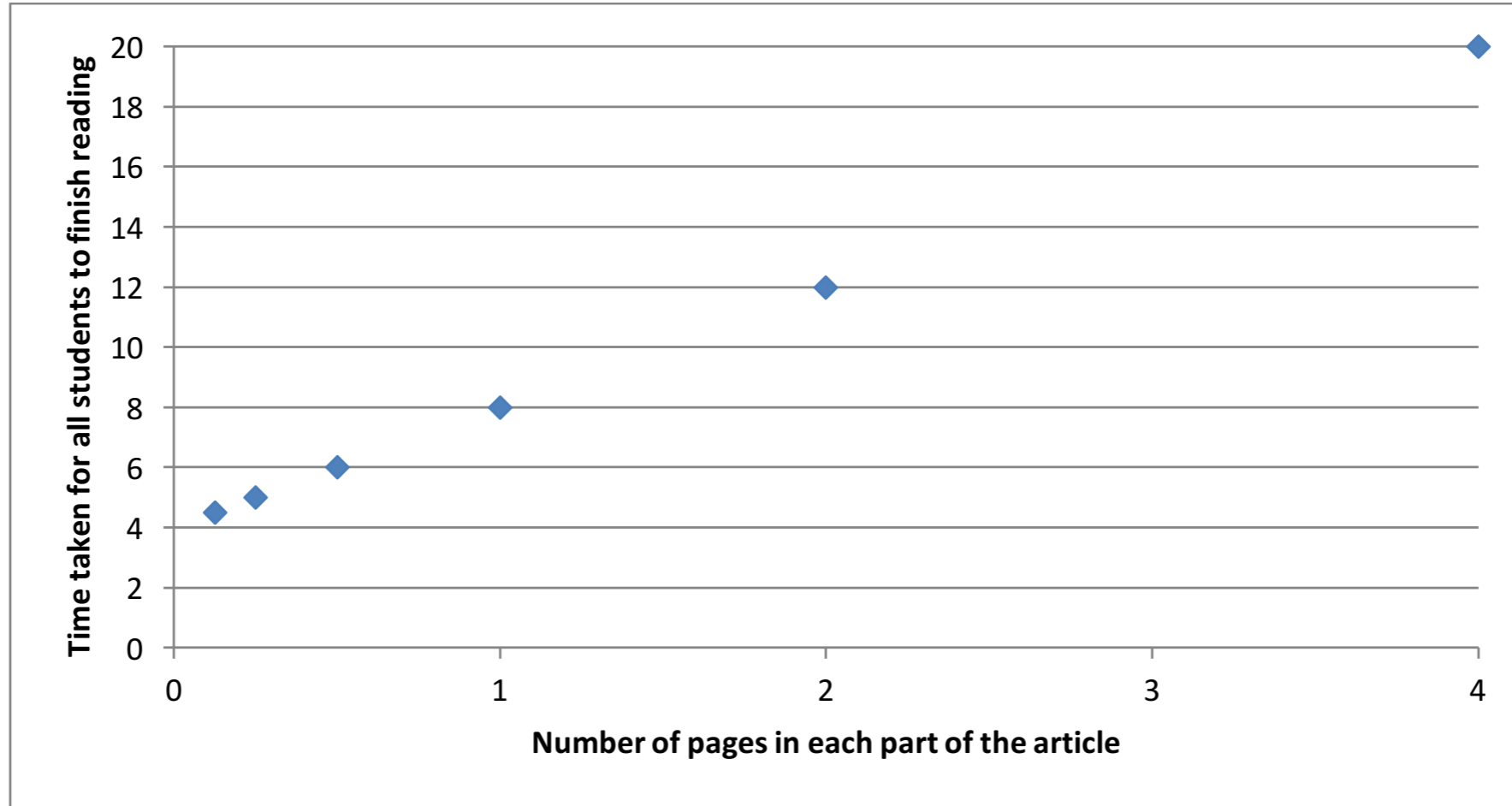


Figure 4: A comparison of total time for five students to finish reading a four page article, assuming each student reads one page per minute and that each passing step takes zero time, when the article is in one 4-

- Diminishing returns — less improvement as we go to smaller and smaller sections

# Examples of Pipelining

## *Student inputs*

- A class reading a book
- Dishwashing: wash, dry, put-away
- Assembly lines
- Microprocessor instruction processing (steps)
- Streaming over multiple network hops (Netflix)
- Graduation ceremony tasks
- Bucket brigade
- Blaze pizza — pizza ordering/production
- Optimized scheduling of workers/tasking a project or organization
- supply chain management

# Examples of Pipelining

Table 1: Correspondence between the above three example scenarios.

	<b>Students reading an article</b>	<b>Truck assembly line</b>	<b>Microprocessor processing instructions</b>
1	The article read by <u>one student</u>	<u>One truck's assembly completed</u>	<u>One instruction processed</u>
2	Partitioning <u>an article</u> into $k$ parts	Partitioning the task of <u>assembling a truck</u> into $k$ assembly steps	Partitioning the task of <u>processing one instruction</u> into $k$ sub-tasks
3	<u>A part of the article</u> read by one student (P1, P2, ...)	<u>A stage of the assembly line</u> works on one truck (A1, A2, ...)	<u>A hardware module performs a sub-task</u> for one instruction (M1, M2, ...)
4	$A_i$ : $i^{\text{th}}$ student completes reading the article	$T_i$ : Assembly of $i^{\text{th}}$ truck completed	$I_i$ : Processing of $i^{\text{th}}$ instruction completed
5	$A_{ij}$ : $i^{\text{th}}$ student completes reading the $j^{\text{th}}$ part of the article	$T_{ij}$ : $j^{\text{th}}$ step in the assembly of $i^{\text{th}}$ truck completed	$I_{ij}$ : $j^{\text{th}}$ sub-task in processing of $i^{\text{th}}$ instruction completed

# Overview

- Explore the concept of pipelining through an example
  - Group reading
- **Some reality checks**
  - Refining our models
  - Limitations of pipelinings
- Characterizing general pipelining approaches



# Discussion: Limitations of Pipelining/Model

- *What has our model neglected?*
- *What can go wrong or what are costs associated with this speed-up?*

# Discussion: Limitations of Pipelining/Model

## *Student inputs*

- *Assumed each student read at the speed*
- *Limited by your slowest processing stage (e.g., slowest reader)*
- *Single point of failure*
- *Need multiple processing resources*
- *Didn't count transition time (e.g., time to hand pages to neighbor)*
- *Cost of ripping the book into pieces*
- *How to build a car in 20 stages? Break an instruction into many sub-steps?*
- *Coordination or time synchronization*
- *Cost to flush a long pipeline — switching costs.*

# Finite Transition Delay

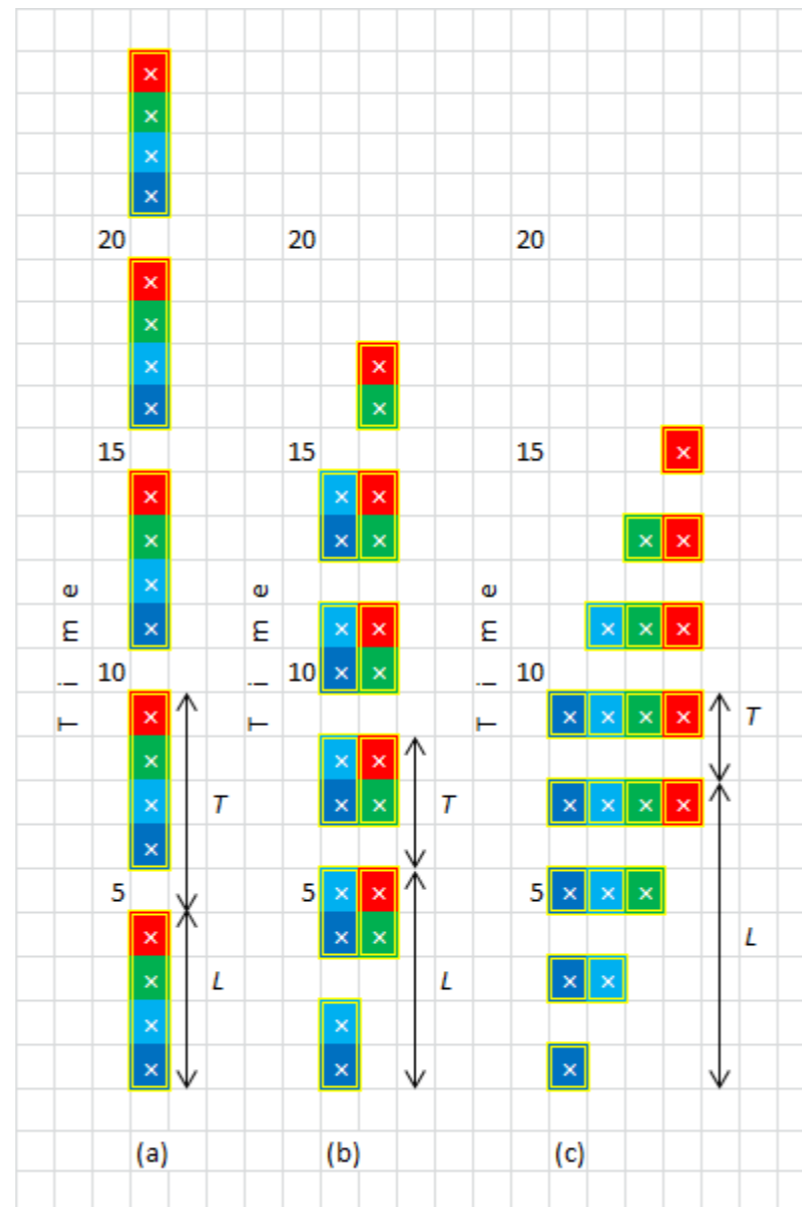


Figure 5: Five students reading one copy of a four-page article at the rate of 1 page per minute, where each passing step has overhead of  $\delta = 1$  minute. Each box with four squares, two squares, or one square shows a part of the article, and each  $\times$  indicates the page being read by a student at the particular time indicated by the y-axis. The empty boxes between reading steps are due to the 1 minute time overhead of each passing step. (a) Full article read and then passed (non-pipelined, baseline for comparison); (b) article divided into two two-page parts, each part read and then passed (pipelined); (c) article divided into four one-page parts, each part read and then passed (pipelined, more extensively than (b)). (For scenarios in (b) and (c), Figure 1 and Figure 3 respectively describe which part is being read by which student at what time.)

# Throughput vs Latency

- *X time units to complete (mins)*
- *Each student requires Y time units to complete*
- *Time between one student and the next finishing is Z time units (mins)*

Latency

Throughput